

the  $\text{IO}_2\text{F}_2^-$  ion seems to increase when a formal positive charge is placed on iodine in iodyl compounds and polymerization may occur not only *via* polycation formation as speculated previously<sup>11,14,21</sup> but also *via* bridging anionic groups. It is obvious that under such circumstances the calculation of iodine-oxygen stretching force constants is not too meaningful.

An additional difference in chemical behavior between  $\text{IO}_2\text{F}$  and  $\text{IO}_2\text{SO}_3\text{F}$  was found when attempts were made to prepare the  $\text{KIO}_2\text{F}_2$  analog  $\text{KIO}_2(\text{SO}_3\text{F})_2$  *via* the reaction  $\text{KIO}_3 + \text{S}_2\text{O}_8\text{F}_2 \rightarrow \text{KIO}_2(\text{SO}_3\text{F})_2 + 0.5\text{O}_2$ . Even though a reaction took place and the white reaction product obtained analyzed as  $\text{KIO}_2(\text{SO}_3\text{F})_2$ , the recorded Raman spectrum revealed the presence of a stoichiometric mixture of  $\text{KSO}_3\text{F}$  and  $\text{IO}_2\text{SO}_3\text{F}$ . This indicates that  $\text{IO}_2\text{SO}_3\text{F}$  does not act as an  $\text{SO}_3\text{F}^-$  acceptor. This conclusion should have some bearing on the interpretation of the conductometric results.

It became interesting to see whether a strongly ionizing solvent as  $\text{HSO}_3\text{F}$  would be capable of breaking up the polymeric structure of  $\text{IO}_2\text{SO}_3\text{F}$ . Quite in contrast to other fluorosulfates which have been studied by us, iodyl fluorosulfate dissolves extremely slowly. Even for small amounts, several hours is required before a clear solution is formed. A similar observation was made when the polymeric solute  $\text{Sn}(\text{SO}_3\text{F})_4$ <sup>28</sup> was dissolved, indicating a slow breaking up of a polymeric species.

The solutions of  $\text{IO}_2\text{SO}_3\text{F}$  were found to be conducting and the maximum concentration was about  $4 \times 10^{-2}$  mol/kg, comparable to the concentration range studied by Gillespie and Senior.<sup>14</sup> The resulting experimental and interpolated electrical specific conductivities are

listed in Table IV for both  $\text{IO}_2\text{SO}_3\text{F}$  and the reference base  $\text{KSO}_3\text{F}$ . A specific conductivity plot *vs.* molality is shown in Figure 3. The following features are noteworthy. Compared to  $\text{KSO}_3\text{F}$  and  $\text{ClO}_2\text{SO}_3\text{F}$ ,<sup>21</sup> iodyl fluorosulfate is not completely dissociated into  $\text{IO}_2^+_{\text{solv}}$  and  $\text{SO}_3\text{F}^-$ , even at very low concentrations. The observed  $\kappa$  values indicate a more extensive ionic dissociation than observed for  $\text{HIO}_3$  in  $\text{H}_2\text{SO}_4$ ,<sup>14</sup> which may well be due to the higher acidity of  $\text{HSO}_3\text{F}$ . The specific conductance *vs.* molality plot shows appreciable curvature. Even though addition of  $\text{KSO}_3\text{F}$  results in an immediate increase in specific conductance—no minimum is observed—the slope of the resulting curve is less steep than that found for  $\text{KSO}_3\text{F}$  itself, indicating some uptake of  $\text{SO}_3\text{F}^-$  and a repression of the original ionic dissociation presumably under formation of  $\text{SO}_3\text{F}$ -bridged polymeric cationic fragments.

In conclusion our experimental findings are in good agreement with previous work by Gillespie and Senior.<sup>14</sup> In addition to the proposed polymeric oxygen-bridged structures,<sup>14</sup> a structural model where discrete  $\text{IO}_2$  groups are bridged by bidentate fluorosulfate groups becomes a possible alternative, which can account for the observed conductivities. Unfortunately no meaningful Raman spectra could be obtained on such dilute solutions.

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## The Crystal Structure of $\beta$ -Yttrium Triantimonide, a Low-Temperature Phase<sup>1</sup>

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A previously reported phase  $\text{Yb}_5\text{Sb}_2$  is shown to be a low-temperature polymorph of  $\text{Yb}_5\text{Sb}_3$ .  $\beta$ - $\text{Yb}_5\text{Sb}_3$  crystallizes in the orthorhombic system, space group  $Pnma$ ,  $a_0 = 12.398$  (2) Å,  $b_0 = 9.562$  (2) Å, and  $c_0 = 8.246$  (2) Å,  $Z = 4$ ,  $\rho_{\text{calcd}} = 8.343$  g/cm<sup>3</sup>. Molybdenum radiation was used to measure the integrated intensities of 1555 independent reflections with a scintillation counter and a four-circle diffractometer. The parameters were refined by least squares to  $R = 0.0797$  for 1252 reflections greater than  $\sigma$  using anisotropic temperature factors. The structure consists of trigonal prisms formed by Yb whose centers are occupied by Sb. The prisms articulate by edge sharing into hexagons, and by face sharing they form hexagonal columns parallel to [010]. Within the columns are rhombs formed by two Yb and two Sb, and the Sb atoms are shared with the next rhombs to produce an infinite chain. The structure is very closely related to  $\text{Rh}_5\text{Ge}_3$ . The shortest Yb-Yb bond length is 3.543 Å and the shortest Yb-Sb distance is 3.044 Å. There is only a tenuous relationship between the structures of the high-temperature  $\alpha$  form and the low-temperature  $\beta$  form.

### Introduction

Seven intermediate phases have been reported to exist in the Yb-Sb phase diagram,<sup>2</sup> and five had known crystal structures. The stoichiometries of the two phases

whose structures were new were given as  $\text{Yb}_5\text{Sb}_4$  and  $\text{Yb}_5\text{Sb}_2$ . A single-crystal structure determination showed that the former compound had the composition  $\text{Yb}_{11}\text{Sb}_{10}$  and was isostructural with  $\text{Ho}_{11}\text{Ge}_{10}$ .<sup>3,4</sup> A pre-

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TABLE I  
 ATOMIC PARAMETERS FOR  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> (PARAMETERS  $\times 10^4$ )

| Atom  | $x$                  | $y$      | $z$      | $B_{11}^a$ | $B_{22}$ | $B_{33}$ | $B_{12}$ | $B_{13}$ | $B_{23}$ |
|-------|----------------------|----------|----------|------------|----------|----------|----------|----------|----------|
| Yb(1) | 740 (1) <sup>b</sup> | 421 (1)  | 1952 (2) | 24 (1)     | 18 (1)   | 30 (2)   | -1 (1)   | -9 (1)   | -0 (1)   |
| Yb(2) | 2295 (1)             | 1/4      | 8196 (2) | 15 (1)     | 28 (2)   | 30 (3)   | 0        | -5 (1)   | 0        |
| Yb(3) | 54 (1)               | 1/4      | 5354 (2) | 14 (1)     | 27 (2)   | 20 (2)   | 0        | 1 (1)    | 0        |
| Yb(4) | 2883 (1)             | 1/4      | 3492 (2) | 15 (1)     | 33 (2)   | 29 (2)   | 0        | -4 (1)   | 0        |
| Sb(1) | 4834 (2)             | 1/4      | 5786 (3) | 14 (1)     | 16 (2)   | 19 (3)   | 0        | -4 (2)   | 0        |
| Sb(2) | 3293 (1)             | 4856 (2) | 675 (2)  | 14 (1)     | 20 (2)   | 26 (2)   | -1 (1)   | 3 (1)    | -3 (2)   |

<sup>a</sup> Coefficients in the temperature factor:  $\exp[-(B_{11}h^2 + B_{22}k^2 + B_{33}l^2 + 2B_{12}hk + 2B_{13}hl + 2B_{23}kl)]$ . <sup>b</sup> The number in parentheses is the standard error in terms of the last significant digit, as derived from the variance-covariance matrix.

liminary report on the structure of Yb<sub>5</sub>Sb<sub>3</sub><sup>5</sup> indicated that, from a consideration of unit cell volume and density, there could be 28–32 atoms in the cell; this range of atoms was within experimental error of the preparation of the compound, and there was an indication of a homogeneity range for this phase. We have determined the crystal structure of this phase and find that the stoichiometry corresponds to Yb<sub>5</sub>Sb<sub>3</sub>. This material is thus a low-temperature form of the previously reported Yb<sub>5</sub>Sb<sub>3</sub> phase which has the D8<sub>8</sub> (Mn<sub>5</sub>Si<sub>3</sub>) structure type.

### Experimental Section

The preparation of this material has been previously described.<sup>2</sup> Small single crystals can be selected from the reaction product without difficulty. An acicular crystal of  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> with dimensions 0.146  $\times$  0.026  $\times$  0.039 mm was mounted on a computer-controlled Picker four-circle goniostat, set at a 4° takeoff angle, and three-dimensional diffraction intensities to  $2\theta = 60^\circ$  were measured with a scintillation-counter detector using unfiltered Mo K $\alpha$  radiation. The lattice constants were determined from a least-squares refinement of 12 Mo K $\beta$  reflections ( $\lambda(\text{Mo K}\beta) = 0.63225 \text{ \AA}$ ) in the range  $2\theta = 20\text{--}30^\circ$ , yielding  $a_0 = 12.398 (2)$ ,  $b_0 = 9.562 (2)$ , and  $c_0 = 8.246 (2) \text{ \AA}$ ,  $Z = 4$ ,  $\rho_{\text{calcd}} = 8.343 \text{ g/cm}^3$ . A total of 1555 independent reflections were measured of which 1252 were greater than  $\sigma$  and 923 were greater than  $2\sigma$ ;  $\sigma$  is the estimated standard error of each individual reflection. An angular scan range of  $1.0^\circ$  was step scanned in increments of  $0.01^\circ$  with 2-sec counts at each step, and the background was measured on each side of the peak for 120 sec. A standard reflection, (400), was used throughout the data collection to check on intensity drift. One measurement of the standard intensity was assigned unit value and all others were expressed as fractions of this value. The intensities obtained between two successive measurements of the standard reflection were multiplied by the appropriate fraction so that all measured intensities were referred to a single value of the (400) intensity. The data were corrected for Lorentz and polarization effects and for absorption ( $\mu = 577.69 \text{ cm}^{-1}$ ).<sup>6</sup> The diffraction symmetry is  $mmm$  and the conditions for reflection are  $hkl0$ ,  $h = 2n$ , and  $0kl$ ,  $k + l = 2n$ , which is consistent with space groups  $Pnma$  and  $Pn2_1a$ . A Wilson plot indicated that the structure was probably centric and the structure confirms this assumption.

### Structure Determination

Initial parameters for about two-thirds of the atoms in the asymmetric unit were determined from an  $E$  map calculated from  $E(hkl)$ 's whose signs were determined by a direct-method program. The program determines signs by iterative application of Sayre's equation and was written by Long.<sup>7</sup> The positions of all of the atoms were determined from Fourier and difference Fourier maps and the structure was refined by a least-squares procedure using a modification of ORFLS.<sup>8</sup> The quantity minimized was  $\sum w(F_o^2 - F_c^2)^2$  with weights,  $w$ , equal to the reciprocals

of the variances which were estimated from the empirical equation

$$\sigma^2(F_o)^2 = [T + B + [0.03(T - B)]^2]/A(Lp)^2$$

where  $T$  is the total count,  $B$  is the background count,  $A$  is the absorption, and  $Lp$  is the Lorentz-polarization expression.<sup>9</sup> The atomic scattering factors for Yb and Sb were taken from Cromer and Waber<sup>10</sup> and the anomalous dispersion terms for Mo K $\alpha$  radiation were taken from Cromer.<sup>11</sup> Table I contains the final atomic parameters obtained from a least-squares refinement based on 1252 reflections greater than  $\sigma$ . The discrepancy indices for the final structure factors, Table II,<sup>12</sup> are as follows: for all 1555 reflections,  $R = 0.100$ ,  $wR = 0.134$ ; for 1252 reflections greater than  $\sigma$ ,  $R = 0.0797$ ,  $wR = 0.133$ ; for 923 reflections greater than  $2\sigma$ ,  $R = 0.0599$ ,  $wR = 0.127$   $\{R = \sum |F_o| - |F_c| / \sum |F_o|, wR = [\sum w(F_o^2 - F_c^2)^2]^{1/2} / [\sum (F_o^2)^2]^{1/2}\}$ . The standard deviation of an observation of unit weight  $[\sum w(F_o - F_c)^2 / (n_0 - n_v)]^{1/2}$  is 1.92 where  $n_0 = 1252$  is the number of reflections and  $n_v$  the number of variables, 44. An extinction correction was applied to  $F_c$  by the method suggested by Zachariasen.<sup>13</sup> A refinement using the acentric space group  $Pn2_1a$  yielded discrepancy indices for the various groups of reflections that were 0.02–0.025 higher than for the comparable centric refinements.

### Discussion

The structure of this alloy can be described in terms of layers of atoms perpendicular to [010]. Yb(1) and Sb(2) atoms form one such layer between  $y = -0.04$  and  $+0.04$ . The Sb(2) atoms form hexagons whose edge is about 4.4  $\text{\AA}$  and their centers are at the centers of inversion. Within each hexagon and symmetrically disposed about the center of inversion are two Yb(1) atoms. Within this layer each Sb(2) is surrounded by three Yb(1) atoms at distances of 3.34, 3.35, and 3.62  $\text{\AA}$ . The distance between the two Yb(1) atoms within the hexagonal ring is 3.79  $\text{\AA}$ . This layer of Yb(1) and Sb(2) atoms is sandwiched between two layers of atoms consisting of Yb(2), Yb(3), Yb(4), and Sb(1), at  $y = +1/4$  and  $y = -1/4$ . The Yb atoms within a level form distorted triangles whose edges vary from 3.62 to 4.43  $\text{\AA}$  and they in turn share corners to form distorted hexagons. Within a hexagon, but offset from the center, is one Sb(1) atom. Within a layer, Yb(2) is surrounded by two Yb(3) atoms at 3.624 and 3.635  $\text{\AA}$ , two Yb(4) atoms at 3.947 and 4.428  $\text{\AA}$ , and two Sb(1) atoms at 3.165 and 3.723  $\text{\AA}$ ; Yb(3) is surrounded by five neighbors consisting of two Yb(4) atoms at 3.829 and 4.160  $\text{\AA}$  and two Yb(2) atoms and one Sb(1) atom at 3.195  $\text{\AA}$ ; Yb(4) has five nearest neighbors consisting of two Yb(2) atoms, two Yb(3) atoms, and one Sb(1) atom at 3.071  $\text{\AA}$ ;

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(12) Table II, a listing of structure factor amplitudes, will appear immediately following this article in the microfilm edition of this volume of the journal. Single copies may be obtained from the Reprint Department, ACS Publications, 1155 Sixteenth St., N.W., Washington, D. C. 20036, by referring to author, title of article, volume, and page number. Remit check or money order for \$3.00 for photocopy or \$2.00 for microfiche.

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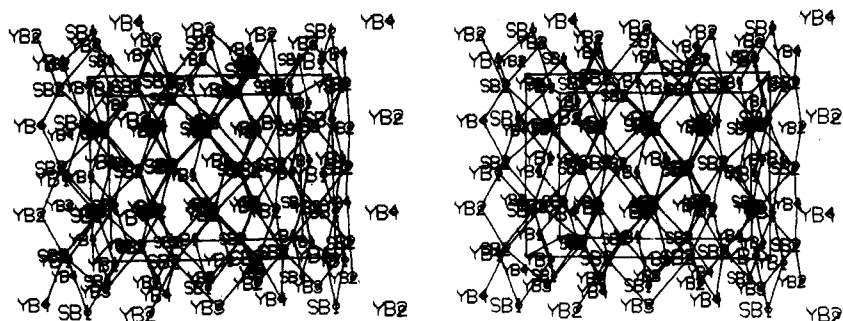


Figure 1.—Stereoscopic view of  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub>. The  $a_0$  axis is horizontal and  $b_0$  is vertical.

the Sb(1) atom has four Yb near neighbors. The layer at  $y = -1/4$  has the same arrangement and is related by inversion centers to the  $y = 1/4$  level.

The Yb atoms in the layers  $y = 1/4$  and  $-1/4$  form trigonal prisms and the Sb(2) atoms in the  $y \cong 0$  level are approximately at the centers of these prisms. The edge of the prism parallel to  $[010]$  is equal to  $1/2b$ . The three-dimensional framework that is formed by this arrangement consists of hexagonal columns parallel to the  $b$  axis and within the hexagonal column is a chain of rhombs formed by Yb(1) and Sb(1) atoms parallel to the  $b$  axis, Figure 1. The rhombs formed by the Sb(1)–Yb(1) atoms are 3.04 and 3.21 Å on edge, the Sb(1)–Yb(1)–Sb(1) angle is  $105.4^\circ$ , and the Yb(1)–Sb(1)–Yb(1) angle is  $74.6^\circ$ . Table III lists bond distances

The solution of the structure fixes the stoichiometry of this previously designated Yb<sub>5</sub>Sb<sub>2</sub> phase as a low-temperature form of Yb<sub>5</sub>Sb<sub>3</sub> which is now labeled as the  $\beta$  form. In the  $D_{8h}$  structure the metalloid atoms form a very distorted octahedron with a metal atom in the center, and these link to form hexagonal columns parallel to  $[001]$ . Within the columns are octahedra of metal atoms. In the  $\beta$  form trigonal prisms are formed by the metal atoms and the array of atoms inside the hexagonal columns is different. Thus a similarity between the two structures can only be introduced if the atomic species which make up the three-dimensional framework are ignored (or interchanged).

The diamond-shaped chain of Yb(1) and Sb(1) atoms in the channels of the  $\beta$  structure could be considered as nonessential to the stability of the structure and the removal of some of the atoms could account for the range of homogeneity that was considered to exist for this compound. In the refinement of the structure the occupancy factors for these two sites were varied and invariably the refinement terminated with full occupancy. Any attempt to vary the scattering power in those sites always resulted in significantly larger discrepancy indices. Thus it is concluded that the crystal which was analyzed had the 5:3 stoichiometry. The previously indicated range of homogeneity might be misleading since in the preparation from the elements some of the starting materials might not participate in the reaction because of their volatility. After the structure was established, we synthesized this material from a 5:3 starting mixture of Yb–Sb and obtained powder patterns identical with the one previously published.<sup>2</sup> Several preparations in which the ratios of the starting components varied always produced materials which gave the  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> powder diffraction pattern, and only when the starting composition exceeded 37.5% Sb was the presence of Yb<sub>4</sub>Sb<sub>3</sub> detected. It must, therefore, be concluded that this is a low-temperature phase with stoichiometry Yb<sub>5</sub>Sb<sub>3</sub> and that it is probably a line compound.

TABLE III

BOND DISTANCES IN  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub><sup>a</sup>

| Atoms       | Dist, Å   | Atoms       | Dist, Å   |
|-------------|-----------|-------------|-----------|
| Yb(1)–Sb(1) | 3.039 (2) | Yb(2)–Sb(2) | 3.284 (2) |
| Yb(1)–Sb(1) | 3.211 (3) | Yb(2)–Sb(2) | 3.353 (2) |
| Yb(1)–Sb(2) | 3.340 (2) | Yb(2)–Yb(3) | 3.624 (2) |
| Yb(1)–Sb(2) | 3.346 (2) | Yb(2)–Yb(3) | 3.634 (3) |
| Yb(1)–Yb(3) | 3.542 (2) | Yb(2)–Sb(1) | 3.722 (3) |
| Yb(1)–Yb(4) | 3.553 (2) | Yb(2)–Yb(4) | 3.947 (3) |
| Yb(1)–Sb(2) | 3.620 (2) | Yb(3)–Sb(1) | 3.194 (4) |
| Yb(1)–Yb(3) | 3.702 (2) | Yb(3)–Sb(2) | 3.250 (2) |
| Yb(1)–Yb(1) | 3.792 (3) | Yb(3)–Sb(2) | 3.266 (2) |
| Yb(1)–Yb(2) | 3.846 (2) | Yb(3)–Yb(4) | 3.829 (3) |
| Yb(1)–Yb(1) | 3.975 (3) | Yb(4)–Sb(1) | 3.071 (3) |
| Yb(1)–Yb(4) | 4.078 (2) | Yb(4)–Sb(2) | 3.275 (3) |
| Yb(2)–Sb(1) | 3.165 (3) | Yb(4)–Sb(2) | 3.430 (2) |

<sup>a</sup> Numbers in parentheses are standard deviations.

around the atoms and they are similar to those observed in other Yb–Sb phases.<sup>2,3</sup> The crystal structure of this phase is almost identical with that of Rh<sub>5</sub>Ge<sub>3</sub><sup>14,15</sup> except that there are slight distortions in Yb<sub>5</sub>Sb<sub>3</sub> which cause the  $a_0$  axis dimension to be larger than would be expected merely because of the change in size of the respective atoms.

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